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### Abstract

This paper proposes the integration and analysis of a closed-loop model of the baroreflex and cardiovascular systems, focused on a time-varying estimation of the autonomic modulation of heart rate in Brugada syndrome (BS), during exercise and subsequent recovery. Patient-specific models of 44 BS patients at different levels of risk (symptomatic and asymptomatic) were identified through a recursive evolutionary algorithm. After parameter identification, a close match between experimental and simulated signals (mean error = 0.81%) was observed. The model-based estimation of vagal and sympathetic contributions were consistent with physiological knowledge, enabling to observe the expected autonomic changes induced by exercise testing. In particular, symptomatic patients presented a significantly higher parasympathetic activity during exercise, and an autonomic imbalance was observed in these patients at peak effort and during post-exercise recovery. A higher vagal modulation during exercise, as well as an increased parasympathetic activity at peak effort and a decreased vagal contribution during post-exercise recovery could be related with symptoms and, thus, with a worse prognosis in BS. This work proposes the first evaluation of the sympathetic and parasympathetic responses to exercise testing in patients suffering from BS, through the recursive identification of computational models; highlighting important trends of clinical relevance that provide new insights into the underlying autonomic mechanisms regulating the cardiovascular system in BS.

<b>Keywords</b>	Autonomic nervous system; Brugada syndrome; computational model; recursive identification
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# Recursive Model Identification for the Analysis of the Autonomic Response to Exercise Testing in Brugada Syndrome

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## Abstract

This paper proposes the integration and analysis of a closed-loop model of the baroreflex and cardiovascular systems, focused on a time-varying estimation of the autonomic modulation of heart rate in Brugada syndrome (BS), during exercise and subsequent recovery. Patient-specific models of 44 BS patients at different levels of risk (symptomatic and asymptomatic) were identified through a recursive evolutionary algorithm. After parameter identification, a close match between experimental and simulated signals (mean error = 0.81%) was observed. The model-based estimation of vagal and sympathetic contributions were consistent with physiological knowledge, enabling to observe the expected autonomic changes induced by exercise testing. In particular, symptomatic patients presented a significantly higher parasympathetic activity during exercise, and an autonomic imbalance was observed in these patients at peak effort and during post-exercise recovery. A higher vagal modulation during exercise, as well as an increased parasympathetic activity at peak effort and a decreased vagal contribution during post-exercise recovery could be related with symptoms and, thus, with a worse prognosis in BS. This work proposes the first evaluation of the sympathetic and parasympathetic responses to exercise testing in patients

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## 1. Introduction

Brugada syndrome (BS) is an inherited disorder presenting a distinctive electrocardiographic pattern associated with an elevated risk for sudden cardiac death (SCD) [1]. Major cardiac events in this population typically occur at  
5 rest and mainly at night, suggesting that the autonomic nervous system (ANS) function, and more specifically the parasympathetic activity, may play a relevant role in the pathophysiology, arrhythmogenesis and prognosis of the disease [2, 3, 4].

However, previous studies on the ANS function of BS patients have led to  
10 conflicting results, particularly when based on long-term measurements. Krit-tayapong et al. concluded that BS patients showed a decreased heart rate variability (HRV) and vagal tone at night compared to controls; as well as a lower diurnal and higher overnight heart rate (HR) when symptomatic patients were compared to asymptomatic subjects and controls [5]. Likewise, Hermida  
15 et al. found significantly lower HRV values at night on symptomatic patients [6]; and Pierre et al. observed a decreased HRV in BS patients, with respect to healthy subjects [7]. Results from Tokuyama et al. also showed a significant HRV reduction on BS patients with respect to controls, as well as on both sympathetic and parasympathetic tones and on their circadian variation over  
20 24 hours [8].

In a previous study from our team [9], although symptomatic BS patients showed a decreased heart rate variability and complexity at night, with respect to asymptomatic subjects, no significant differences were observed be-

tween groups on sympathetic and parasympathetic modulations. On the other  
 25 hand, in Nakazawa et al., results showed higher vagal and reduced sympathetic  
 tones in symptomatic BS patients [10]. Likewise, in a recent work from Be-  
 har et al., symptomatic subjects showed an increased parasympathetic activity  
 during both daytime and nighttime, when compared to asymptomatic patients  
 [11]. Finally, HRV analysis in Kostopoulou et al. did not reveal any significant  
 30 difference between BS patients and controls [12].

Thus, in order to better characterize autonomic modulation, standard ma-  
 neuvers such as exercise testing can be applied. Exertion causes a sympathetic  
 activation that, together with a parasympathetic inhibition, increases HR, a  
 reliable indicator to evaluate cardiac autonomic function [13]. Conversely, post-  
 35 exercise cardiodeceleration is adjusted by parasympathetic activation and sym-  
 pathetic withdrawal [14]. Indeed, some studies have already reported the po-  
 tential of exercise testing in BS [15, 16, 17, 18]. Amin et al. [19] found a higher  
 parasympathetic reactivation during early recovery after exertion in BS patients  
 with prior ventricular fibrillation events. Likewise, Makimoto et al. concluded  
 40 that a higher vagal activity after exercise was related to the occurrence of cardiac  
 events in BS [20].

Although classical temporal and spectral markers are widely used in clini-  
 cal practice for ANS analysis [21], conventional methods have failed to estimate  
 sympathetic and parasympathetic responses to exercise, even in healthy subjects  
 45 [22], but also in Brugada syndrome patients [18, 23]. Nevertheless, since compu-  
 tational models can directly represent interactions between the cardiovascular  
 system (CVS) and the ANS, model-based reasoning could provide useful knowl-  
 edge to support autonomic response interpretation in BS. Indeed, in a previous  
 work, we already reported the feasibility of the application of such computa-  
 50 tional models to reproduce cardiovascular data acquired during head-up tilt  
 testing on a healthy subject and on a BS patient [24]. However, the identifi-  
 cation method applied to the system-level models used in this work could only  
 explain the mechanical, circulatory and autonomic sympathetic functions of the  
 cardiovascular system. To tackle this limitation, high-frequency oscillations in-

55 duced by the parasympathetic regulation of the ANS can be estimated through recursive identification.

Therefore, in this work we propose a novel approach based on the recursive identification of a closed-loop mathematical model of the baroreflex and cardiovascular systems, in order to estimate the time-varying sympathetic and parasympathetic contributions to HR modulation during exercise and subsequent recovery on Brugada patients. Patient-specific models were adjusted for 44 BS patients with different levels of risk (13 symptomatic and 31 asymptomatic) so as to reproduce their HR during exercise testing and, thus, analyze their underlying autonomic function. The paper is organized as follows: in section 2, the experimental protocol and data under study are presented, the computational model is described and the recursive identification method is explained. In section 3, the results of applying the described methods are presented and discussed. Conclusions are finally specified in section 4.

## 2. Material and Methods

### 70 2.1. Study population

The standard 12-lead ECG recordings from 44 patients diagnosed with BS who took part in a physical stress test were collected during a multicentric study conducted in the Cardiology department of the Rennes University Hospital (France). Participants were enrolled in 6 French hospitals located in Rennes, Saint Pierre de la Reunion, Nantes, Bordeaux, Brest and La Rochelle. The study protocol was approved by the respective local ethics committees and all patients provided written informed consent before participation.

In accordance with current guidelines [25], BS was diagnosed when a coved ST-segment elevation ( $\geq 0.2$  mV) was identified in at least one right precordial lead (V1 and/or V2) located in the 2<sup>nd</sup>, 3<sup>rd</sup> or 4<sup>th</sup> intercostal space, in the presence or absence of sodium-channel-blocking agent.

In order to characterize populations with different levels of risk, patients were classified as symptomatic or asymptomatic, based on their medical his-

tory. Thirteen patients presented documented symptoms of ventricular origin:  
85 syncope (61.5%), cardiac arrest (38.5%) and dizziness (15.4%), whereas the re-  
remaining 31 patients were considered as asymptomatic.

Patients age ranged from 19 to 74 years old ( $45.07 \pm 12.59$  years old) and  
33 (75%) were males. ICD implantation had been performed in 6 of 31 (19.4%)  
asymptomatic patients, based on a positive EPS test, whereas all symptomatic  
90 patients were ICD carriers. Among 31 patients (11 were symptomatic) in whom  
genetic screening was performed, an *SCN5A* mutation was found in 13 (41.9%),  
from whom 6 were symptomatic.

Table 1 summarizes the clinical characteristics of patients included in the  
study. Since all between-groups differences, apart from ICD implantation, were  
95 statistically non-significant, similar baseline characteristics were assumed be-  
tween populations.

Table 1: Clinical characteristics of BS patients.

	<b>Symptomatic</b>	<b>Asymptomatic</b>	<b><i>p</i>-value</b>
	<b>(n=13)</b>	<b>(n=31)</b>	
<b>Age, years old</b>	43.62 $\pm$ 14.51	45.68 $\pm$ 11.90	0.322
<b>Male sex, <i>n</i> (%)</b>	11 (84.6%)	22 (71%)	0.355
<b>ICD implantation, <i>n</i> (%)</b>	13 (100%)	6 (19.4%)	<0.001
<b><i>SCN5A</i> mutation, <i>n</i> (%)</b>	6 (46.2%)	5 (25%)	0.311

Values are mean  $\pm$  standard deviation or number of observations (%).

Comparisons are based on Mann-Whitney U non-parametric tests.

## 2.2. Experimental protocol and data

Participants underwent a triangular exercise test recommended by the Amer-  
ican Heart Association [26], which was performed on a cyclo ergometer (Ergoline  
100 900 Egamed, Piestany, Slovakia) and divided in the following phases, repre-  
sented in Fig. 1:

- Exercise phase:

- Warm-up phase: for men, initial load of 50 watts (W); for women, initial load of 30 W, both for 2 minutes.
- 105 – Incremental exercise phase: for men, initial load of 80 W for 2 minutes and then incrementing 20 W every 2 minutes; for women, initial load of 50 W, increasing 20 W every 2 minutes. For each patient, the load was increased until it reached the 80% of his/her theoretical maximum heart rate, defined by the formula  $MHR = 220 - age$  [27].
- 110 • Recovery phase: for men, fixed load of 50 W; for women, fixed load of 30 W, both for 3 minutes.

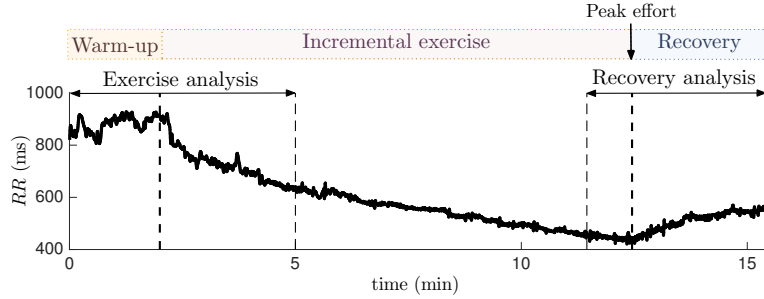


Figure 1: Representative example of RR-interval series observed during the exercise test. The test was divided in three phases: warm-up, incremental exercise and recovery. Due to differences in exercise durations for each patient, recursive identifications were separately performed at the beginning and at the end of the test (exercise and recovery analysis, respectively). Exercise analysis included the warm-up phase and the first 3 minutes of incremental exercise; while recovery analysis was based on the last minute of exertion before peak effort and the recovery phase.

ECG data were acquired with the Holter monitor (ELA medical, Sorin Group, Le Plessis Robinson, France) at a sampling frequency of 1000 Hz. From these signals, RR-interval series were extracted from the lead presenting the  
 115 highest signal-to-noise ratio (SNR), by means of a noise-robust wavelet-based algorithm for QRS-complex detection and subsequent R-wave peak location [28]. Since the result is a non-uniformly sampled signal, a cubic-spline interpolation was applied to RR-interval time series, to obtain regularly sampled data at a

rate of 10 Hz, which was the sample rate chosen for the model.

### 2.3. Computational model

Based on our previous works in cardiovascular modeling [29, 30, 31, 24], the proposed model was composed of two coupled submodels representing the cardiovascular system (CVS) and the baroreceptors reflex system (BRS), connected through the HR resulting from the BRS submodel and the systemic arterial pressure coming from the CVS.

#### 2.3.1. Cardiovascular system

As illustrated in Fig. 2, the hemodynamic effects of exercise testing were represented by implementing the cardiovascular model defined in [32].

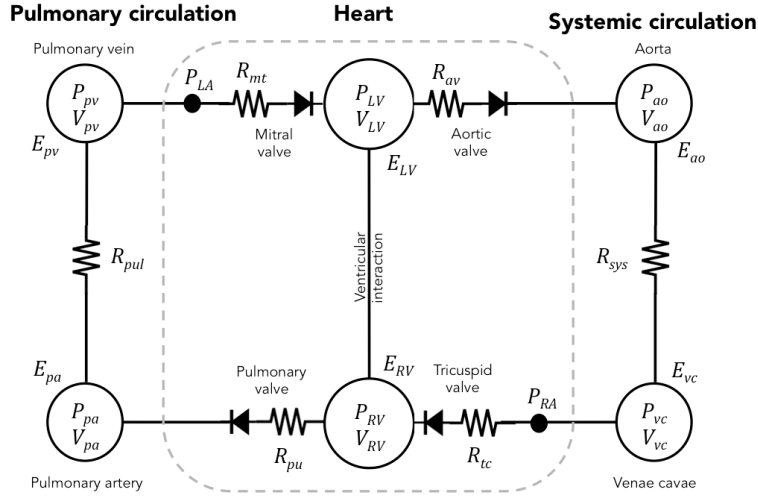


Figure 2: Closed-loop model of the cardiovascular system. E: elastance; R: resistance; P: pressure; V: volume; sys: systemic; pul: pulmonary; pv: pulmonary vein; pa: pulmonary artery; pu: pulmonary valve; av: aortic valve; tc: tricuspid valve; mt: mitral valve; ao: aorta; vc: venae cavae; LA: left atrium; LV: left ventricle; RA: right atrium; RV: right ventricle.

Volumes ( $V$ ) from each cardiac chamber are obtained from the integral of their respective net flows ( $Q_{in} - Q_{out}$ ). Blood pressure ( $P$ ) is then computed



from the pressure-volume relationships associated with systole ( $P_{es}$ ) and diastole ( $P_{ed}$ ), and a periodic function ( $e(t)$ ) drives the transition between these relationships as follows:

$$P(V, t) = e(t)P_{es}(V) + (1 - e(t))P_{ed}(V), \quad (1)$$

$$P_{es}(V) = E \cdot (V - V_d), \quad (2)$$

$$P_{ed}(V) = P_0 \cdot (\exp[\lambda(V - V_0)] - 1), \quad (3)$$

$$e(t) = A \cdot \exp[-B \cdot ((t - t_s) - C)^2]. \quad (4)$$

135  $E$  refers to the systolic elastance and  $V_d$  is the dead volume, respectively representing the slope and intercept of the linear pressure-volume relationship associated with systole. During diastole, this relationship is non-linear and is described by a gradient ( $P_0$ ), a curvature ( $\lambda$ ) and a volume at zero pressure ( $V_0$ ). Eq. 4 defines the transition between diastolic and systolic dynamics,  
140 modulated by a Gaussian function with amplitude  $A$ , width  $B$  and center  $C$ ; and  $t_s$  refers to the cardiac cycle onset, determined by the HR resulting from the BRS submodel.

Atria were not included in the model since they minimally contribute to main cardiac trends. However, in order to account for relevant ventricular in-  
145 teractions, ventricles were coupled through the septum, represented as a flexible common wall between left and right ventricles. The left ventricle (LV) free wall volume ( $V_{LVf}$ ) and the right ventricle (RV) free wall volume ( $V_{RVf}$ ) are defined as:

$$V_{LVf} = V_{LV} - V_{spt}, \quad (5)$$

$$V_{RVf} = V_{RV} + V_{spt}. \quad (6)$$

where  $V_{spt}$ ,  $V_{LV}$  and  $V_{RV}$  are respectively the septum, LV and RV volumes.  
150 Then, the septum volume results from linking the septum pressure ( $P_{spt}$ ) to the difference between left and right ventricular pressures:

$$P_{spt} = P_{LV} - P_{RV} , \quad (7)$$

$$P_{spt} = e(t)E_{spt} \cdot (V_{spt} - V_{d,spt}) \quad (8)$$

$$+(1 - e(t))P_{0,spt}(\exp[\lambda(V - V_0)] - 1). \quad (9)$$

Diodes simulate the one-way direction of blood when passing through valves located at the inlet and exit of ventricles. Pressures on the peripheral circulation systems are calculated as a linear relationship between their volume and vascular  
155 elastance, following eq. 2. Finally, flows between chambers are obtained from the equation  $Q = \frac{\Delta P}{R}$ , where  $\Delta P$  is the pressure gradient between two chambers and  $R$  accounts for the corresponding vascular resistance connecting them.

### 2.3.2. Baroreflex model

Sympathetic and parasympathetic efferent responses to arterial blood pressure regulation were modeled based on a widely used approach [33, 34], represented in Fig. 3.  
160

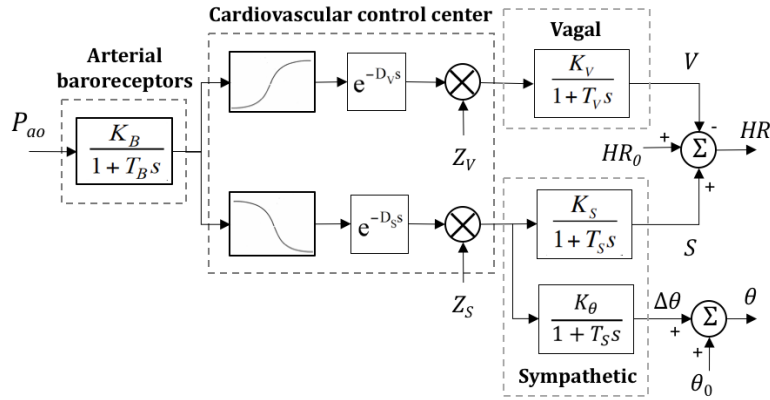


Figure 3: Diagram of the baroreflex model for cardiovascular regulation. From the arterial pressure registered at the systemic circulation ( $P_{ao}$ ), the baroreflex system controls heart rate ( $HR$ ) and other cardiovascular variables ( $\theta$ ), such as ventricular contractility or elastance, systemic resistance and venous dead volume.

The systemic arterial pressure registered at the CVS submodel was used as

the input pressure for the baroreflex system which, in turn, modulated the HR used as input of the CVS submodel, thus defining the closed-loop model.

165 Baroreceptors dynamical properties are represented by a first-order transfer function, whose gain and time constant are  $K_B$  and  $T_B$ . Then, cardiovascular control is represented, in both sympathetic and vagal branches, by a sigmoidal function and delays  $D_S$  and  $D_V$ , respectively. Sympathetic and parasympathetic contributions are modulated by two time-varying variables,  $Z_S$  and  $Z_V$ ,  
 170 to account for the influence of exogenous phenomena and collect all the variability caused by sources other than blood pressure fluctuations (central modulation, respiration, etc.).

For chronotropic regulation, each efferent pathway is finally modeled with a first-order filter, characterized by a gain ( $K_V$ ,  $K_S$ ) and a time constant ( $T_V$ ,  $T_S$ ).  
 175 The output HR is the result of adding the contributions of both sympathetic ( $S$ ) and vagal ( $V$ ) branches to the intrinsic heart rate ( $HR_0$ ):

$$HR = HR_0 + S - V. \quad (10)$$

Finally, other sympathetic branches control ventricular contractility ( $E$ ), systemic resistance ( $R$ ) and venous dead volume ( $VV$ ) through a first-order filter characterized by the sympathetic time constant  $T_S$  and the gain related  
 180 to each branch  $K_\theta$ , where  $\theta \in \{E, R, VV\}$ . Being  $\theta_0$  the baseline response and  $\Delta\theta$  the baroreflex regulation, the output response for each regulated variable is defined as:

$$\theta = \theta_0 + \Delta\theta. \quad (11)$$

#### 2.4. Recursive identification

All model parameters other than  $Z_S$  and  $Z_V$  were fixed based on the literature [32, 33, 35]. Their values are provided as Supplementary material (Tables  
 185 I and II).

As illustrated in Fig. 4, at each step  $i$  of the recursive algorithm, parameters  $Z_S$  and  $Z_V$  were identified on a time interval  $T_I$  of duration largely inferior to

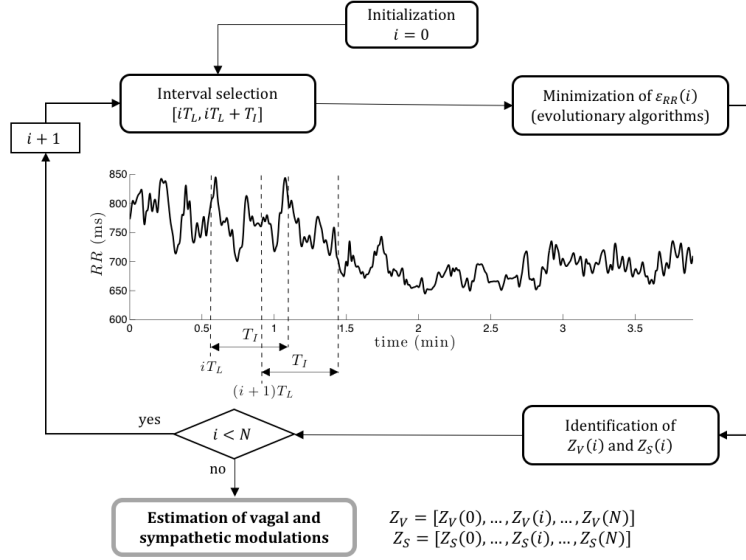


Figure 4: Diagram of the recursive identification algorithm and time windows involved.  $T_L$ : overlap window;  $T_I$ : identification window;  $\epsilon_{RR}$ : error function. For visualization purposes,  $T_L$  and  $T_I$  temporal supports were enlarged in this figure and do not illustrate representative time windows.

the RR-interval series length ( $T_I \ll T_{TOT}$ ). At each step, simulated and  
190 experimental signals were compared in order to minimize the error function  $\epsilon_{RR}(i)$ , defined as:

$$\epsilon_{RR}(i) = \sum_{t_e=iT_L}^{(i+1)T_L} |RR_{sim}(t_e) - RR_{exp}(t_e)| + \sum_{t_e=iT_L}^{iT_L+T_I} |RR_{sim}(t_e) - RR_{exp}(t_e)|, \quad i \in [0, \dots, N] \quad (12)$$

where  $t_e$  is the time elapsed since the onset of the identification period,  $T_L$  corresponds to the overlap time between each interval and  $N = \lfloor T_{TOT}/T_L \rfloor$  is the number of identification intervals. The time windows involved in the  
195 recursive identification algorithm are also represented in Fig. 4.

The overlap time duration  $T_L$  was set equal to the parasympathetic time

constant ( $T_V$ ) to capture rapid fluctuations due to vagal response; whereas interval  $T_I$  was set as the sympathetic time constant ( $T_S$ ) in order to take into account the low frequency component causing RR-interval series slow variations.

200 As in previous works of our team [36, 37], the best set of  $\{Z_S, Z_V\}$  parameters for each patient was identified on each interval  $i$ , through an approach based on evolutionary algorithms [38]. The initial population, or first set of candidate optimization solutions, was randomly generated. For the following steps, assuming limited parameter variations between intervals, the initial population  
 205 was set equal to that obtained from the previous interval  $i - 1$ . Although this approach limits parameter variations, mutation probability was set to  $p_m = 0.2$  in order to stimulate the exploration of the entire search space and prevent from convergence to local minima.

These recursive identifications were separately performed during exercise  
 210 and recovery. Since each patient test differed in the incremental exercise phase duration and the shortest case in our clinical series lasted less than 5 minutes, as represented in Fig. 1, for exercise analysis, only the warm-up phase and the first 3 minutes of incremental exertion were identified. Then, for recovery analysis, the last minute of exertion and the first 3 minutes of recovery, were assessed.

215 In order to quantify identification performance, the error between simulated and experimental RR-interval series for both exercise ( $E_{exercise}$ ) and recovery ( $E_{recovery}$ ) phases was expressed in percentage and computed as:

$$E = \frac{1}{n} \sum_{i=1}^n |100 \cdot \frac{RR_{sim}(i) - RR_{exp}(i)}{RR_{exp}(i)}|, \quad (13)$$

where  $n$  is the number of samples being compared. Due to identification errors caused by initialization, the first minute of warm-up was removed from exercise  
 220 analysis, as well as the first 30 seconds of the last minute of exertion were eliminated from recovery analysis.

### 2.5. Statistical analysis

The identified time-varying sympathetic ( $S$ ) and parasympathetic ( $V$ ) contributions to exercise and subsequent recovery were then compared between

225 symptomatic and asymptomatic patients, by Mann-Whitney U non-parametric tests. In order to compare the last minute of exertion and recovery, all patients were synchronized with respect to the peak effort instant.

The autonomic response to exercise testing was also analyzed by fitting linear regression models to the estimated  $S$  and  $V$  of each patient, for the last minute  
 230 of warm-up, the first, second and third minutes of incremental exercise, the last 30 seconds of exertion, and the first, second and third minutes of recovery.

### 3. Results and Discussion

Based on visual inspection and error results ( $E_{exercise} = 1.10 \pm 0.54\%$ ,  $E_{recovery} = 0.52 \pm 0.16\%$ ), a satisfactory agreement was observed between simulated signals and real data, leading to errors always inferior to 3.5%. Fig. 5  
 235 illustrates an example of simulated and experimental RR-interval series during the last minute of warm-up and the first 3 minutes of incremental exercise ( $E = 1.7\%$ ).

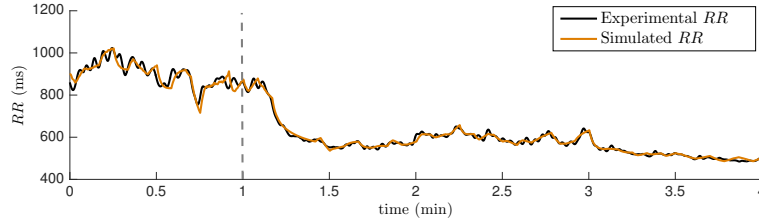


Figure 5: Simulated (orange) and experimental (black) RR-interval series during the last minute of warm-up and the first 3 minutes of incremental exercise.  $E = 1.7\%$ . The dashed vertical line delimits the end of warm-up and subsequent incremental exercise onset.

Fig. 6 shows the mean vagal and sympathetic contributions of the autonomic response to exertion, for symptomatic and asymptomatic patients. In  
 240 both groups, vagal modulation remained low along the whole exercise phase and decreased as the test progressed. Conversely, sympathetic contribution increased during exercise, and specially after warm-up. Moreover, symptomatic patients presented significantly higher parasympathetic values around the sec-

245 ond minute of incremental exercise, and mainly at the end of warm-up, where this group also presented significantly higher sympathetic values.

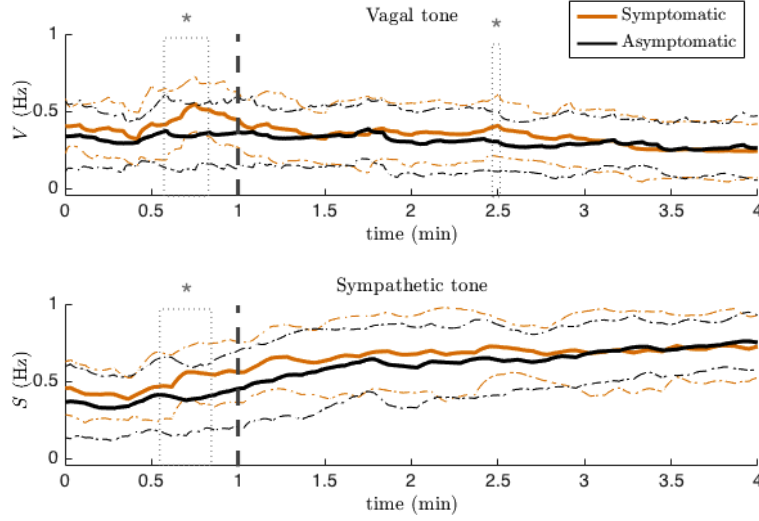


Figure 6: Mean estimation of vagal ( $V$ ) and sympathetic ( $S$ ) contributions, for symptomatic (orange) and asymptomatic (black) patients, during exercise. Dashed vertical lines delimit the end of warm-up and subsequent incremental exercise onset. Pointed boxes indicate those segments where significant differences between groups ( $*p < 0.05$ ) were found. Dashed horizontal lines represent the standard deviations for each group.

These results are in agreement with those found in the literature, where a higher vagal modulation has been observed in symptomatic BS patients [11, 10]. Although some significant differences were also found after 1 minute of incremental exercise, the largest and most significant segment was observed at the end of warm-up. Moreover, sympathetic activity in this phase was also found to be higher in symptomatic patients, contrary to tendencies found in previous publications based on classical spectral markers [8, 10]. Nevertheless, many studies on cardiac autonomic function based on classic approaches have failed to represent the sympathetic response to exercise testing, even in healthy subjects [22], since the LF component does not provide an index of sympathetic tone but rather reflects a complex interplay among many factors including the sympathetic and parasympathetic contributions to ANS. Similarly, our previous works

based on conventional time-frequency methods failed to estimate the autonomic  
 260 response to exercise testing in this population [18, 23]. Thus, model-based rea-  
 soning may provide better estimations of the sympathetic and parasympathetic  
 contributions to HR modulation during exercise.

In Fig. 7, the mean vagal and sympathetic contributions during recovery,  
 for symptomatic and asymptomatic patients, are represented. After the peak  
 265 effort, an increase in parasympathetic activity, as well as a decrease in sympa-  
 thetic modulation can be observed for both groups. Although no statistically  
 significant differences related to symptomatic status were found on the vagal  
 modulation, at the end of the second minute of recovery, symptomatic patients  
 presented significantly lower sympathetic values. These findings concur with a  
 270 previous work where a lower sympathetic activity was reported in symptomatic  
 patients [10].

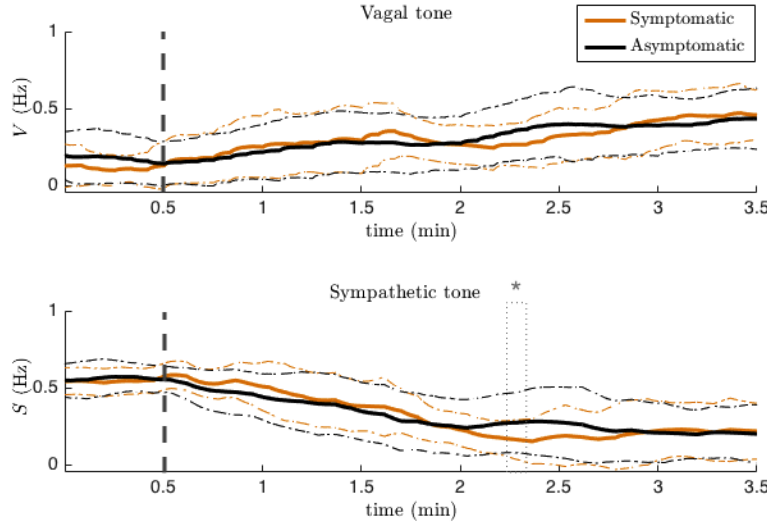


Figure 7: Mean estimation of vagal ( $V$ ) and sympathetic ( $S$ ) contributions, for symptomatic (orange) and asymptomatic (black) patients, during post-exercise recovery. Dashed vertical lines delimit the end of exertion and subsequent recovery onset. The pointed box indicates the segment where significant differences between groups ( $*p < 0.05$ ) were found. Dashed horizontal lines represent the standard deviations for each group.

Finally, the slopes from the adjusted linear regression models were compared



between symptomatic and asymptomatic populations. Since no statistically significant results were obtained during exercise analysis, Table 2 summarizes, for each analyzed period during recovery, the mean  $\pm$  standard deviation values obtained for each group of patients, together with their associated  $p$ -values.

Table 2: Mean  $\pm$  standard deviation slopes for sympathetic and parasympathetic contributions (in Hz), and associated  $p$ -values, from symptomatic and asymptomatic patients, at peak effort and during different periods of recovery after exertion ( $*p < 0.05$ ). Comparisons are based on Mann-Whitney U non-parametric tests.

	Symptomatic (n=13)	Asymptomatic (n=31)	$p$ -val
<b>Peak effort (30 sec)</b>			
<i>Sympathetic</i>	0.09 $\pm$ 0.30	-0.03 $\pm$ 0.25	0.26
<i>Parasympathetic</i>	<b>0.09 <math>\pm</math> 0.22</b>	<b>-0.11 <math>\pm</math> 0.25</b>	<b>0.03*</b>
<b>Recovery (1<sup>st</sup> min)</b>			
<i>Sympathetic</i>	-0.21 $\pm$ 0.26	-0.18 $\pm$ 0.27	0.72
<i>Parasympathetic</i>	0.15 $\pm$ 0.29	0.15 $\pm$ 0.25	0.82
<b>Recovery (2<sup>nd</sup> min)</b>			
<i>Sympathetic</i>	-0.22 $\pm$ 0.22	-0.02 $\pm$ 0.35	0.05
<i>Parasympathetic</i>	<b>-0.03 <math>\pm</math> 0.18</b>	<b>0.16 <math>\pm</math> 0.33</b>	<b>0.04*</b>
<b>Recovery (3<sup>rd</sup> min)</b>			
<i>Sympathetic</i>	0.13 $\pm$ 0.40	-0.11 $\pm$ 0.51	0.12
<i>Parasympathetic</i>	0.26 $\pm$ 0.46	-0.01 $\pm$ 0.51	0.11

Symptomatic and asymptomatic patients showed significant differences in vagal modulation, when compared at peak effort and during the second minute of recovery. Fig. 8 illustrates the mean slope for symptomatic and asymptomatic populations at peak effort and during recovery, highlighting those segments where significant differences were found.

Although results show non-negligible standard deviations, on average, the simulated vagal contribution was consistent with physiological knowledge on asymptomatic patients, decreasing at peak effort and increasing during post-

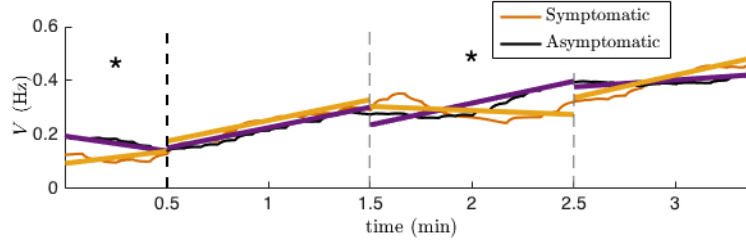


Figure 8: Mean linear regression models adjusted to the estimation of vagal modulation at peak effort and during post-exercise recovery, for symptomatic (orange) and asymptomatic (black) patients. Dashed vertical lines delimit the analyzed periods and segments presenting statistically significant differences between populations are noted (\* $p < 0.05$ ).

285 exercise recovery. However, significant alterations were noted on symptomatic patients, showing a mean positive slope at peak effort and a descending trend during the second minute of recovery.

Thus, these findings provide further evidence for the role of autonomic imbalance in the pathophysiology of BS. However, since this study is based on a relatively small population of 44 BS patients, the moderately significant differences found between analyzed groups should be interpreted carefully. Indeed, the fact that corrected  $p$ -values would lead to non-significant results, indicates that reliable physiological interpretations should be extracted by means of larger clinical series. Moreover, the analyzed population presents a significant imbalance between symptomatic and asymptomatic groups; although this is a common scenario in BS, where symptoms refer to recovered SCD or syncope and, thus, they are usually found in a small amount of patients. Likewise, most previously reported studies on BS autonomic function are based on clinical series of similar, or even smaller, sizes [5, 6, 10, 7, 12, 8], as well as most works reporting the identification of computational models are based on small populations.

Thus, the implemented model-based approach provides the first time-varying autonomic estimation in the context of BS, highlighting the relevance of exercise testing in order to unmask significant changes in ANS modulation that may not be captured at daytime, during a regular ECG examination. Indeed, this

305 altered autonomic cardiac system dynamics during post-exercise recovery, when  
vagal contribution is predominant, concurs with previous studies reporting an  
increase in Brugada-like ECG changes induced during vagal stimulation [39],  
as well as with the fact that most life-threatening cardiac arrhythmias in BS  
occur at rest and during sleep, when parasympathetic activity is predominant  
310 [40, 2]. Furthermore, the results confirm previous findings where symptomatic  
BS patients showed a higher vagal modulation [11, 10, 8] with respect to asymp-  
tomatic patients, supporting the idea that increased vagal responses could be  
related to a worse prognosis in Brugada syndrome.

#### 4. Conclusions

315 Conventional methods have been proved insufficient for autonomic function  
analysis. Therefore, in this work, we propose an original model-based approach  
to characterize ANS dynamics in response to exertion. It is based on a recur-  
sively identified closed-loop model of the baroreflex and cardiovascular systems,  
introducing: i) patient-specific model parameter recursive identifications and ii)  
320 estimations of the time-varying sympathetic and parasympathetic modulations  
of the heart rate.

The model was evaluated with data from 44 BS patients, acquired during  
exercise testing, to compare the autonomic function of symptomatic and asymp-  
tomatic BS populations. Results show a close match between experimental and  
325 simulated signals. Moreover, estimations of sympathetic and parasympathetic  
components were consistent with physiological knowledge, showing the feasibil-  
ity of the model to reproduce realistic autonomic responses to exercise.

According to results, a significantly higher parasympathetic activity was ob-  
served in symptomatic patients during exercise, providing further evidence for  
330 the role of vagal contribution in BS prognosis. Moreover, during post-exercise  
recovery, parasympathetic modulation on symptomatic patients indicated an  
autonomic imbalance. Thus, this original approach enables to unmask indica-  
tors capturing cardiovascular and autonomic dynamics, never before studied in

BS, that may be useful for risk stratification. Indeed, we believe that a robust  
335 BS risk stratification should be based on a combination of both classical electro-  
physiological features, but also on this kind of markers providing an improved  
estimation of the autonomic activity.

More extensive evaluations including a wider range of parameters, a greater  
population of patients, as well as the possibility of adjusting parameters based  
340 on not only the HR, but also the blood pressure, should be performed in the  
future. Furthermore, the proposed model could be enriched by including a  
representation of cardiorespiratory interactions [33].

Nevertheless, this paper presents the first model-based approach towards the  
evaluation of the time-varying autonomic response to exertion in BS patients,  
345 showing results that indicate trends of clinical relevance and, thus, provide a  
step forward towards the understanding of the disease.

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TABLE I  
CVS SUBMODEL PARAMETER VALUES.

Parameter	Description	Nominal value
$E_{ao}$	Aorta elastance (mmHg ml <sup>-1</sup> )	0.705
$E_{vc}$	Venae cavae elastance (mmHg ml <sup>-1</sup> )	0.011
$E_{pa}$	Pulmonary artery elastance (mmHg ml <sup>-1</sup> )	0.338
$E_{pv}$	Pulmonary vein elastance (mmHg ml <sup>-1</sup> )	0.006
$E_{LVf}$	Left ventricle free wall elastance (mmHg ml <sup>-1</sup> )	3.405
$E_{RVf}$	Right ventricle free wall elastance (mmHg ml <sup>-1</sup> )	0.653
$E_{spt}$	Septum elastance (mmHg ml <sup>-1</sup> )	48.754
$V_{d,ao}$	Aorta dead volume (ml)	800
$V_{d,vc}$	Venae cavae dead volume (ml)	2830
$V_{d,pa}$	Pulmonary artery dead volume (ml)	160
$V_{d,pv}$	Pulmonary vein dead volume (ml)	200
$V_{d,LVf}$	Left ventricle free wall dead volume (ml)	5
$V_{d,RVf}$	Right ventricle free wall dead volume (ml)	5
$V_{d,spt}$	Septum dead volume (ml)	2
$V_{0,pcd}$	Pericardium end-diastolic volume (ml)	200
$V_{0,LVf}$	Left ventricle free wall end-diastolic volume (ml)	5
$V_{0,RVf}$	Right ventricle free wall end-diastolic volume (ml)	5
$V_{0,spt}$	Septum elastance end-diastolic volume (ml)	2
$\lambda_{pcd}$	Pericardium end-diastolic exponent (ml <sup>-1</sup> )	0.030
$\lambda_{LVf}$	Left ventricle free wall end-diastolic exponent (ml <sup>-1</sup> )	0.015
$\lambda_{RVf}$	Right ventricle free wall end-diastolic exponent (ml <sup>-1</sup> )	0.015
$\lambda_{spt}$	Septum end-diastolic exponent (ml <sup>-1</sup> )	0.435
$P_{0,pcd}$	Intrinsic pericardium pressure (mmHg)	0.500
$P_{0,LVf}$	Intrinsic left ventricle free wall pressure (mmHg)	1.275
$P_{0,RVf}$	Intrinsic right ventricle free wall pressure (mmHg)	1.200
$P_{0,spt}$	Intrinsic septum pressure (mmHg)	1.110
$A$	Amplitude of Gaussian transition function (n.u.)	1
$B$	Width of Gaussian transition function (n.u.)	80
$C$	Center of Gaussian transition function (n.u.)	0.4
$R_{mt}$	Mitral valve resistance (mmHg s ml <sup>-1</sup> )	0.001
$R_{av}$	Aortic valve resistance (mmHg s ml <sup>-1</sup> )	0.011
$R_{tc}$	Tricuspid valve resistance (mmHg s ml <sup>-1</sup> )	0.001
$R_{pu}$	Pulmonary valve resistance (mmHg s ml <sup>-1</sup> )	0.004
$R_{pul}$	Pulmonary circulation resistance (mmHg s ml <sup>-1</sup> )	0.143
$R_{sys}$	Systemic circulation resistance (mmHg s ml <sup>-1</sup> )	1.050
$V_{tot}$	Total blood volume (ml)	5500
$P_{pt}$	Thoracic cavity pressure (mmHg)	-4

TABLE II  
BRS SUBMODEL PARAMETER VALUES.

Parameter	Description	Nominal value
$HR0$	Intrinsic heart rate (Hz)	1.33
$K_B$	Baroreceptors gain (n.u.)	1
$T_B$	Baroreceptors time constant (s)	2
$K_V$	Gain for vagal heart rate modulation (n.u.)	1
$T_V$	Vagal time constant (s)	1.5
$a_V$	Normalization offset for vagal heart rate modulation (n.u.)	0
$b_V$	Normalization gain for vagal heart rate modulation (n.u.)	1
$M_V$	Normalization center for vagal heart rate modulation (n.u.)	100
$\lambda_V$	Normalization exponent for vagal heart rate modulation (n.u.)	-0.04
$D_V$	Vagal delay (s)	0.2
$K_S$	Gain for sympathetic heart rate modulation (n.u.)	1
$T_S$	Sympathetic time constant (s)	8
$a_S$	Normalization offset for sympathetic heart rate modulation (n.u.)	0
$b_S$	Normalization gain for sympathetic heart rate modulation (n.u.)	1
$M_S$	Normalization center for sympathetic heart rate modulation (n.u.)	100
$\lambda_S$	Normalization exponent for sympathetic heart rate modulation (n.u.)	0.09
$D_S$	Sympathetic delay (s)	2
$K_R$	Gain for peripheral resistance modulation (n.u.)	1
$T_R$	Peripheral resistance time constant (s)	8
$a_R$	Normalization offset for peripheral resistance modulation (n.u.)	0
$b_R$	Normalization gain for peripheral resistance modulation (n.u.)	1
$M_R$	Normalization center for peripheral resistance modulation (n.u.)	100
$\lambda_R$	Normalization exponent for peripheral resistance modulation (n.u.)	0.09
$D_R$	Peripheral resistance delay (s)	2
$K_{VV}$	Gain for venous volume modulation (n.u.)	1
$T_{VV}$	Venous volume time constant (s)	8
$a_{VV}$	Normalization offset for venous volume modulation (n.u.)	0
$b_{VV}$	Normalization gain for venous volume modulation (n.u.)	1
$M_{VV}$	Normalization center for venous volume modulation (n.u.)	100
$\lambda_{VV}$	Normalization exponent for venous volume modulation (n.u.)	0.09
$D_{VV}$	Venous volume delay (s)	2
$K_E$	Gain for contractility/elastance modulation (n.u.)	1
$T_E$	Contractility time constant (s)	8
$a_E$	Normalization offset for contractility modulation (n.u.)	0
$b_E$	Normalization gain for contractility modulation (n.u.)	1
$M_E$	Normalization center for contractility modulation (n.u.)	100
$\lambda_E$	Normalization exponent for contractility modulation (n.u.)	0.09
$D_E$	Contractility delay (s)	2